A man is known to speak the truth 3 out of 4 times. He throws a die and reports that it is a six. The probability that it is actually a six is,

(A)
$$\frac{3}{8}$$
 (B) $\frac{1}{5}$ (C) $\frac{3}{4}$ (D) None of these

Solution

Let E be the event of occurrence of 6.

Then,
$$P(E) = \frac{1}{6}, P(\overline{E}) = \frac{5}{6}$$

Let A be the event of man reporting the number to be 6.

Then, $P(A/E) = \frac{3}{4}$ as A/E means he is reporting 6 as 6 or he is telling the truth.

 $P(A/\overline{E}) = \frac{1}{4}$ as A/\overline{E} means he is not telling the truth.

Using Bayes' theorem, $P(E/A) = \frac{P(E)P(A/E)}{P(E)P(A/E) + P(\overline{E})P(A/\overline{E})}$

$$\therefore P(E / A) = \frac{\frac{1}{6} \times \frac{3}{4}}{\frac{1}{6} \times \frac{3}{4} + \frac{5}{6} \times \frac{1}{4}} = \frac{3}{8}$$

Hence, (A)