

The displacement of a particle executing periodic motion is given by $y = 4 \cos^2\left(\frac{t}{2}\right) \sin(1000t)$.

Which of the following is NOT an independent constituent simple harmonic motion?

(A) $\sin 999t$

(B) $\sin 1000t$

(C) $\sin 1001t$

(D) $2 \sin 1000t$

Solution

We have, $y = 4 \cos^2\left(\frac{t}{2}\right) \sin(1000t)$

Or $y = 2(1 + \cos t) \sin(1000t)$

Or $y = 2 \sin(1000t) + 2 \sin(1000t) \cos t$

Or $y = 2 \sin(1000t) + \sin(1001t) + \sin(999t)$

The three independent constituent simple harmonic motions are evident from above. So, the answer is option (B).