If a satellite is revolving around a planet of mass 'M' in an elliptic orbit of semi-major axis 'a', the orbital speed of the satellite when it is at a distance 'a' from the focus is:

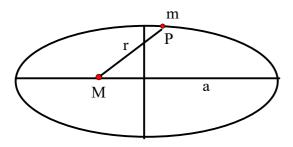
(A)
$$\sqrt{\frac{GM}{a}}$$

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 (B) $\sqrt{\frac{3GM}{a}}$ (C) $\frac{GM}{a}$ (D) $\frac{3GM}{a}$

(C)
$$\frac{GM}{a}$$

(D)
$$\frac{3GM}{a}$$

Solution



$$TME = -\frac{GMm}{2a}$$

Since mechanical energy is conserved,

$$-\frac{GMm}{2a} = \frac{1}{2}mv^2 - \frac{GMm}{r}$$
 at some point P distance r from the focus

$$\therefore v^{2} = GM\left(\frac{2}{r} - \frac{1}{a}\right)$$
When $r = a$, $v^{2} = GM\left(\frac{2}{a} - \frac{1}{a}\right) = \frac{GM}{a}$

$$\therefore v = \sqrt{\frac{GM}{a}}$$

Hence, (A)