

If the vectors $\overline{AB} = 3\hat{i} + 4\hat{k}$ and $\overline{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$ are the sides of a triangle ABC, then the length of the median through A is:

(1) $\sqrt{18}$

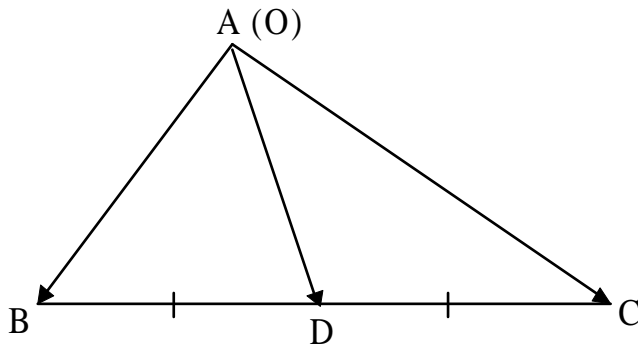
(2) $\sqrt{72}$

(3) $\sqrt{33}$

(4) $\sqrt{45}$

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Solution



Let observer be placed at A, then

\overline{AB} = position vector of B & \overline{AC} = position vector of C

Since D is the mid-point of BC,

position vector of D = $\frac{1}{2}$ (position vector of B + position vector of C)

$$\therefore \overline{AD} = \frac{1}{2}(\overline{AB} + \overline{AC}) = \frac{1}{2}(3\hat{i} + 4\hat{k} + 5\hat{i} - 2\hat{j} + 4\hat{k}) = \frac{1}{2}(8\hat{i} - 2\hat{j} + 8\hat{k}) = 4\hat{i} - \hat{j} + 4\hat{k}$$

$$\therefore AD = \sqrt{4^2 + (-1)^2 + 4^2} = \sqrt{33} \text{unit}$$

Hence, (3).